

BOTTLENECK-BASED HEURISTIC FOR PERMUTATION FLOWSHOP
SCHEDULING

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DEDICATION

To my beloved parents Isa Bin Awang and Siti Hawa Binti Ismail.

Thank You Mom, Dad and Family members

For taking care of me and always standing right behind of me,

Supporting me in whatever decisions I make,

May Allah S.W.T grant all of you a Jannah.

To all my friends

Thank you for everything we shared.

For the laugh, cry and every moments,

I am the luckiest person to have all of you during my up and down.

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May the Al-Mighty God, Allah S.W.T, richly bless all of you.

ABSTRACT

The newly heuristic is developed by introducing the bottleneck-based concept that was applied at the beginning of initial solution determination. The heuristic is known as Bottleneck-Based (BNB) heuristic. The previous study found that the scheduling activity become complex when dealing with large number of machine, $m > 2$, it is NP-hardness. Thus, the main objective of this study are to propose and develop a new heuristic for solving permutation flowshop scheduling by considering four-machines and n -jobs ($n = 6, 10, 15, 20$). Three phases were applied into this study in order to boost the makespan performance of the proposed heuristic. Two phases (bottleneck identification phase and initial sequence arrangement phase) were newly introduced and combined with the existing famous Nawaz, Ensore and Ham (NEH) insertion technique. There are four potential dominant machines (M1, M2, M3, M4) clustered as bottleneck machines. A total 1000 set random processing time for each job sizes was tested using Excel simple programming with built in Visual Basic for Application (VBA). The heuristic performance was evaluated based on the average makespan ratio, average percentage error, and percentage of solution performance obtained. This study considered the NEH heuristic as the best and appropriate tool for comparison purpose since NEH heuristic is the best performing heuristic in minimizing the makespan. The heuristic evaluation result showed that the BNB heuristic is performing better than the NEH at bottleneck machines M1, M3 and M4. While, heuristic verification result showed that the bottleneck algorithms performed the best in minimizing the makespan for set of problems with bottleneck machine M4. However, the overall result showed fluctuate values over the size of jobs. The result of this study shown that the developed BNB heuristic achieved good performance in solving small sized problems however further modification is needed for medium and large sized problems.

ABSTRAK

Heuristik baru ini dihasilkan dengan memperkenalkan kaedah asas kejejalan dimana ia diaplikasikan pada permulaan penentuan penyelesaian awalan. Heuristik ini dikenali sebagai heuristik Berasaskan Kejejalan (BNB). Objektif utama kajian ini dijalankan adalah untuk menghasilkan satu heuristik baru untuk menyelesaikan masalah aliran penjadualan bagi empat-mesin dan n -kerja ($n = 6, 10, 15, 20$). Tiga fasa diaplikasikan dalam kajian ini dalam usaha untuk meningkatkan prestasi masa kerja siap dalam heuristik yang dicadangkan. Dua fasa baru diperkenalkan menggabungkan satu fasa sedia ada iaitu teknik sisipan NEH yang terkenal. Terdapat empat mesin dominan yang berpotensi (M1, M2, M3, M4) yang telah dikelompokkan sebagai mesin kejejalan selepas fasa pengenpastian kejejalan. Semua jumlah 1000 data pemprosesan masa untuk semua saiz kerja telah diuji menggunakan program ringkas Excel dengan aplikasi pengaturcaraan makro Visual Basic (VBA). Prestasi heuristik dinilai berdasarkan nisbah purata masa siap kerja dan peratusan prestasi penyelesaian. Kajian ini mempertimbangkan heuristik NEH sebagai pengukuran yang sesuai untuk tujuan perbandingan memandangkan heuristik NEH merupakan yang paling terbaik dalam mengurangkan masa siap kerja. Keputusan menunjukkan heuristik BNB berprestasi lebih baik daripada NEH di mesin kejejalan M1, M3 dan M4. Sementara, keputusan verifikasi heuristik menunjukkan algoritma BNB berprestasi baik dalam mengurangkan masa siap kerja untuk beberapa set masalah untuk mesin kejejalan M4. Walaubagaimanapun, keseluruhan keputusan menunjukkan nilai yang berubah-ubah bagi setiap saiz kerja. Keputusan kajian ini menunjukkan heuristik ini berprestasi sangat baik dalam menyelesaikan masalah bersaiz kecil tetapi masih memerlukan pengubahsuaian untuk menyelesaikan masalah bersaiz sederhana dan besar.

CONTENTS

RESEARCH TITLE	i
DECLARATION	ii
DEDICATION	iii
ACKNOWLEDGEMENT	iv
ABSTRACT	v
ABSTRAK	vi
CONTENTS	vii
LIST OF TABLES	x
LIST OF FIGURES	xii
LIST OF EQUATIONS	xiii
LIST OF ABBREVIATIONS	xiv
LIST OF APPENDICES	xvi
 CHAPTER 1 INTRODUCTION	 1
1.1 Background of the study	1
1.2 Problem statement	3
1.3 Objectives of the study	4
1.4 Scope of the study	4
1.5 Significant of the study	5
1.6 Thesis layout	5

CHAPTER 2	LITERATURE REVIEW	6
2.1	Introduction	6
2.2	Scheduling	6
2.2.1	Flowshop scheduling	8
2.2.2	Job shop scheduling	9
2.2.3	Open shop scheduling	9
2.3	Permutation flowshop scheduling	10
2.4	Heuristic approach	11
2.4.1	NEH heuristic	16
2.4.2	Bottleneck-based heuristic	17
2.5	Solving scheduling problem with specific objectives	18
2.5.1	Minimization of makespan and flowtime	19
2.5.2	Earliness and tardiness	27
2.6	Summary of the chapter	31
CHAPTER 3	METHODOLOGY	33
3.1	Introduction	33
3.2	Methodology of the study	33
3.3	Data collection	36
3.4	Introduction to simulation program	36
3.4.1	Excel environment, formulation, tolerance	37
3.4.2	VBA coding	37
3.5	BNB heuristic concept	37
3.5.1	Bottleneck machine identification phase	40
3.5.2	Initial sequences phase	42
3.5.2.1	Six-jobs and ten-jobs	42
3.5.2.1	Fifteenth-jobs and twenty-jobs	43
3.5.3	Insertion phase	44
3.6	Simulation experimental design	46
3.7	Summary of the chapter	49
CHAPTER 4	RESULTS ANALYSIS AND DISCUSSION	50
4.1	Introduction	50
4.2	Bottleneck-based heuristic procedure	50

4.2.1	Bottleneck identification phase	51
4.2.2	Initial sequences arrangement phase	52
4.2.3	Job insertion phase	53
4.3	Heuristic performance results	62
4.3.1	Six-jobs	63
4.3.2	Ten-jobs	68
4.3.3	Fifteenth-jobs	71
4.3.4	Twenty-jobs	73
4.4	Discussion on heuristic evaluation results	76
4.5	Heuristic verification	79
4.6	Discussion on heuristic verification results	83
4.7	Summary of the chapter	84

CHAPTER 5 CONCLUSION AND RECOMMENDATION FOR FUTURE WORKS 85

5.1	Introduction	85
5.2	Conclusion	85
5.3	Recommendation for future works	86

REFERENCES 89

APPENDIX 95



LIST OF TABLES

TABLE	TITLE	PAGE
2.1	Summary of heuristic from previous research	15
2.2	Summary of makespan and flowtime from previous research	25
2.3	Summary of earliness and tardiness from previous research	30
2.4	Summary of scheduling topic	32
3.1	Example of average processing time for six-jobs	41
3.2	Example of dominance calculation for six-jobs	42
3.3	Experimental design of generating test problems	46
4.1	Example of processing times	51
4.2	Example of machine dominance calculation	52
4.3	Processing time in descending order	53
4.4	Initial sequences arrangement	53
4.5	Example of first two job sequencing	54
4.6	Example for third job sequencing	55
4.7	Example for fourth job sequencing	56
4.7	Example for fourth job sequencing (continued)	57
4.8	Example for fifth job sequencing	57
4.8	Example for fifth job sequencing (continued)	58
4.8	Example for fifth job sequencing (continued)	59
4.9	Example for sixth job sequencing	60
4.9	Example for sixth job sequencing (continued)	61
4.9	Example for sixth job sequencing (continued)	62
4.10	Machine bottleneck identification for six-jobs	63
4.11	Heuristics evaluation against optimum result	63
4.12	Evaluation of heuristics performance for six-jobs	64
4.13	Machine bottleneck identification for ten-jobs	68
4.14	Evaluation of heuristics performance for ten-jobs	68
4.15	Machine bottleneck identification for fifteenth-jobs	71

4.16	Machine bottleneck identification for fifhtteen-jobs	71
4.17	Machine bottleneck identification for twenty-jobs	73
4.18	Evaluation of heuristics performance for twenty-jobs	74
4.19	Overall performance of heuristic evaluation for all problem sizes	76
4.20	BNB verification for six-jobs	79
4.21	BNB verification for ten-jobs	80
4.22	BNB verification for fifhtteen-jobs	81
4.23	BNB verification for twenty-jobs	82
4.24	Overall performance of heuristic verification for all job sizes	83



LIST OF FIGURES

FIGURE	TITLE	PAGE
2.1	Flowshop scheduling illustrations	8
3.1	Flow chart of heuristic development	35
3.2	720 iterations coding (six-jobs only)	38
3.3	Example of 100 set of random data coding	38
3.4	Optimum answer coding (six-jobs only)	39
3.5	Example of bottleneck machine coding	39
3.6	Example of BNB and NEH makespan coding	40
3.7	Flowchart of insertion phase	45
4.1	Dotplot graph of heuristics performance for six-jobs	65
4.2	BNB/NEH makespan performance for six-jobs	67
4.3	BNB/NEH makespan performance for ten-jobs	70
4.4	BNB/NEH makespan performance for fifhteen-jobs	72
4.5	BNB/NEH Makespan performance for twenty-jobs	72
4.6	Overall performance of BNB average makespan ratio for all job sizes	78

LIST OF EQUATIONS

EQUATION	TITLE	PAGE
3.1	Machine dominant value	41
3.2	BNB makespan Ratio	47
3.3	NEH makespan ratio	47
3.4	Percentage of BNB optimum result	47
3.5	Percentage of NEH optimum result	47
3.6	BNB/NEH makespan ratio	47
3.7	Percentage of BNB makespan equal NEH	48
3.8	Percentage of BNB makespan larger than NEH	48
3.9	Percentage of BNB makespan less than NEH	48
3.10	Percentage of accurate BNB result	48

LIST OF ABBREVIATIONS

NEH	-	Nawaz, Ensore and Ham
VBA	-	Visual Basic for Application
BNB	-	Bottleneck-Based
PFSP	-	Permutation Flowshop Scheduling Problem
NP	-	Non-Deterministically Polynomial
SA	-	Simulated Annealing
CPU	-	Computational Time
CDS	-	Campbell, Dudek and Smith
GA	-	Genetic Algorithm
WY	-	Woo and Yim
RZ	-	Rajendran and Ziegler
FL	-	Framinan and Leisten
GS	-	Gelders and Sambandam
MN	-	Miyazaki and Nishiyama
NEHKK1	-	Nawaz, Ensore and Ham, Kalcynzki and Kombruowski 1
NEH-D	-	NEH based on Deviation
FSMP	-	Flowshop Multiple Processors
CDS1	-	Campbell, Dudek, and Smith 1
PAM	-	Hundal and Rajgopal modified Palmer
CDS2	-	Campbell, Dudek, and Smith 2
HO	-	Ho Heuristic
GLB	-	Global Lower Bound
DC	-	Daniels and Chambers
CR	-	Chakravartyh and Rajendran
DCH	-	Daniels and Chambers Heuristic
SAH	-	Simulated Annealing Heuristic
FSDS	-	Flowshop With Sequence-Dependent Setup Times
PA	-	Percentage Advantage
API	-	Average Percentage Improvement
WPT-MS	-	Weighted Processing Time and Minimum Slack Components

Greedy-ET	-	Greedy-Type Procedure for Earliness or Tardiness
EDD	-	Earliest Due Dates
NEHedd	-	Nawaz, Ensore and Ham Earliest Due Dates
SPT	-	Simple Priority Rule
M1	-	Machine Number 1
M2	-	Machine Number 2
M3	-	Machine Number 3
M4	-	Machine Number 4



LIST OF APPENDICES

APPENDIX	TITLE	PAGE
A	Processing time for six-jobs	96
B	Makespan result for BNB, NEH and optimum	103



PTTA UTHM
PERPUSTAKAAN TUNKU TUN AMINAH

CHAPTER 1

INTRODUCTION

1.1 Background of the study

Scheduling is an act of planning and prioritizing activities with the time limit for the job completion in order to meet with certain requirement, constraints or to achieve the goal of objectives (Emmons and Vairaktarakis, 2012). Since the time always be the greatest constraint, therefore the scheduling becomes very important to organize the activities efficiently and optimally (Xhafa and Abaraham, 2008).

In worldwide industries, scheduling plays an important role in the production system since the resources are becoming more critical to be controlled. The resources are referred to the machine, manpower, material and many more (Chakraborty, 2009). The greatest outcome can be gained if the scheduling of the resources is successfully organized. It was a great advantage to the manufacturer in worldwide industries if the latest successful researches easy to understand and easily applied to the current manufacturing system (Mukhopadhyay, 2015). Hence, efficient scheduling system helps the manufacturer to increase the profit by cutting all the unnecessary cost associated with inefficient scheduling (Sule, 2008).

Scheduling model were categorised into many categories such as flowshop, job shop, open shop and dependent shop (Kalczynski and Kombruowski, 2005). In flowshop scheduling, all the jobs are processed on multiple machines in an identical sequence with same or different processing time. This flowshop scheduling is to reduce or minimize the completion time for all the processed jobs defined as makespan. The processing order of the jobs on the machine is the same for each subsequent step of processing and this is categorised as permutation flowshop scheduling (Marichelvam, 2014).

The permutation flow shop scheduling is a well-known combinatorial optimization problem that arises in many manufacturing systems. Over the last few decades, permutation flowshop problems have widely been studied and solved as a static problem (Rahman *et. al*, 2015). The permutation flowshop scheduling problem became famous and interesting topic among the researchers when Nawaz, Ensore and Ham (NEH) introduced the NEH heuristic around three decade ago where the heuristic was declared as the highest performing method in minimizing the makespan and achieved the answer near to optimum solution (Framinan *et.al*, 2003). Many researchers have modified or used NEH heuristic as a basis to improve the scheduling solutions (Woo and Yim, 1998; Allahverdi and Aldowaisan, 2002; Kalczynski and Kombruowski, 2005; Kalczynski and Kamburowski, 2007; Dong *et. al*, 2007; Saleh, 2014; Isa, 2015). The current available heuristic for permutation flowshop scheduling problem was classified as constructive or improvement methods (metaheuristic). A constructive heuristic builds a sequence of jobs so that once a decision was made, it cannot be reversed. Meanwhile, improvement heuristic starts with any sequence of jobs and then attempts to decrease the value of the objective by amending the sequence. Clearly, an improvement method can be applied to the sequence obtained from a constructive heuristic (Osman and Kelly, 1996). As a continuing effort from the literature, this research is intended to improve the NEH solution and to develop a new constructive heuristic by using bottleneck-based (BNB) approach.

1.2 Problem statement

In the production scheduling system, researchers have found that the scheduling activities became more complex when dealing with more than two machines and it became a NP-hardness problem. Non-deterministic polynomial-time hard known as NP-hardness, in computational complexity theory is defined as a class of problems that are informally said “at least as hard as the hardest problems in NP” (Wegener, 2005). The researches then have focused on the development of implicit enumeration technique. However, it leads to emphasize the development of heuristic to find a near optimal solution for large size problems since implicit enumeration technique have a major constraint that there is the limitation on the problem sized that can be solved by that technique in a reasonable time (Allahverdi and Aldowaisan, 2002). It is the reason on why it is difficult to produce a new heuristic with answer near to optimum solution for a large number of machines and jobs in permutation flowshop scheduling. NEH algorithm appears to be the best heuristic in solving the makespan criterion problem, but it is not wise to just rely on NEH heuristic without further study since the improvement can still be made. Framinan et.al (2003) and Abedinnia *et. al* (2016) recommended further studies to be conducted to the NEH by choosing different sorting criterion beside using the ascending order of indicator values. Thus, this study is about to create a simple heuristic to boost the scheduling performance with the objective of makespan minimization since the previous finding shows that the modification is needed in order to strengthen the heuristic. The idea is by developing a new heuristic for permutation flowshop scheduling using bottleneck-based concept. The bottleneck phenomenon occurs frequently in many manufacturing systems (Chen and Chen, 2009). Identifying bottleneck resources and scheduling the jobs rationally helps in ensuring the feasibility and effectiveness of scheduling result and also help in reducing the difficulty in follow-up scheduling. Zhang and Wu (2012) shows that the local search effort for the bottleneck machines has generate higher quality of solution result and at reasonable short computational time. In this study, the bottleneck concept was applied first as initial solution step before the insertion phase where it was used as an indicator value in identifying the bottleneck machines. Besides that, this study also increases the understanding of bottleneck-based concept by developing computer program that can be used to

robustly test the performance of the algorithms using Visual Basic for Application (VBA) in Microsoft Excel. Since all the data was tabulated in Excel spreadsheet, this research is providing more visible analyses on the performance of the bottleneck-based heuristic in permutation flowshop scheduling.

1.3 Objectives of the study

The objectives for this study are:

1. To propose and develop a new heuristic using bottleneck-based (BNB) concept for permutation flowshop scheduling problem.
2. To analyse the performance of the BNB heuristic in flowshop scheduling environment.

1.4 Scope of the study

The scopes for this study are as follow:

1. Apply bottleneck-based concept for flowshop scheduling using Microsoft Excel.
2. Perform the bottleneck-based concept by using measurement of 4 machines and n -jobs ($n = 6, 10, 15, 20$) in flowshop environment.
3. Measure the makespan performance of the case study by using Excel simple programming in Visual Basic for Application (VBA).
4. The performances of BNB heuristic were compared with the optimum solution ($n = 6$) and NEH heuristic ($n = 6, 10, 15, 20$).

1.5 Significant of the study

Almost all the manufacturing industries used the scheduling planning in their production system daily process. Scheduling heuristic studies is important because:

- i. It helps the industries to minimize the idle time.

When the job sequence was organized properly, the completion time can be reduced as well as the idle time.

- ii. It helps the industries cutting the cost of underutilize skill labour and expensive machines.

A simple programming used in scheduling activities that was easy to conduct can help the industries reduces the operation cost since the programming is well known and low cost.

- iii. It increases the profit gained by the industries.

The industries can reduces the operation cost through good and systematic scheduling activities, thus increasing the profit gained.

- iv. It increases the related literature or academic reports in the field of production scheduling.

Since the scheduling plays an important role in production and manufacturing industries, the latest research helps in guiding the industries and manufacturer in applying efficient scheduling system.

1.6 Thesis layout

The further design of this thesis includes the review of scheduling system and the method used to develop a heuristic by previous researchers in Chapter 2. The methodology on the techniques and procedure used in this case study was highlighted in Chapter 3. The heuristic procedure was briefly discussed, and also the result and discussion of heuristic performance and heuristic verification was presented in Chapter 4. Finally, the research conclusion and recommendation for future works was discussed in Chapter 5.

CHAPTER 2

LITERATURE REVIEW

2.1 Introduction

In this section, a literature review regarding the heuristic algorithm and information related to this topic was collected and reported. All the knowledge gained from the literature contributes in better understanding of the heuristic and also the concept used in this research. In general, this review was divided into subtopics which are scheduling, permutation flowshop scheduling, heuristic approach, solving scheduling problem and lastly a summary of chapter.

2.2 Scheduling

Scheduling is a planning activity with required task and with the time constraints to be performed. It is a decision making process (Marichelvam, 2014). Scheduling is considered as important factor in many manufacturing and services industries (Sule, 2008). According to Mendes (2013), scheduling is one of the most critical issues in the planning and managing of manufacturing process where the difficulty in finding the optimal schedule depends on the shop environment, the process constraint and the performance indicator. Production scheduling problems are faced by thousands of companies worldwide that are engaged in the production of tangible goods. Efficient scheduling leads to increased efficiency, utilization and ultimately, profitability. It is

the reason that has attracted the attention of many practitioners and researchers from both fields of production management and combinatorial optimization in solving the production scheduling problems effectively and efficiently (Xhafa and Abraham, 2008). In the scheduling process, the type and the amount of each resource need to be known so that we can determine when the tasks can feasibly be accomplished. When the resources have been specified, we can effectively define the boundary of the scheduling problem (Kenneth and Dan, 2013). In production planning terminology, scheduling models are divided into some categories known as flowshop, job shop and open shop scheduling.

2.2.1 Flowshop scheduling

In flowshop scheduling, each job processed by a series of machine must have the same sequence even though the processing times may be different. Most authors added the requirement that a job never revisits any stage which can be numbered as $1, 2, \dots, m$, and every job visits them in numerical order. In a pure flowshop each job has m tasks and visits all stages (Emmons and Vairaktarakis, 2012). Generally, jobs may have fewer than m tasks and may skip over some stations. Jobs may skip some machines in a skip-shop (Chakraborty, 2009). There is a certain cases in flowshop identified as re-entrant flowshop which a jobs may recycle and be reprocessed at the same station in multiple times (Ahmad, 2009). But as long as all the jobs followed the same path, the systems is still considered as flowshop.

According to Mukhopadhyay (2015), in a more complex compound flowshop, each machine may be replaced by a set of parallel machines which each job can choose one form the first cluster, one from the second and so on. In a finite queue flowshop there is limited storage in front of machines other than the first. An important special case is when no storage is allowed except at the first machine. For example, in the metal processing industries, that requirement is frequently encountered where the metal is rolled while it is hot. Delays between operations result in cooling, making the rolling operation prohibitively difficult (Thomas and David, 1993). The simple variation of flowshop called as “skip shops”, re-entrant

flowshop”, “compound flowshop”, and “finite queue” flowshop. The illustration may be seen in Figure 2.1. The descriptions of flowshop variation are as follow:

1. Skip shops

Jobs may skip some machines and treated as zero processing time.

2. Re-entrant flowshop

Jobs may repeat the process on certain machine.

3. Compound flowshop

A group machine may replace the machine in the series.

4. Finite queue flowshop

There is limited storage in front of machines.

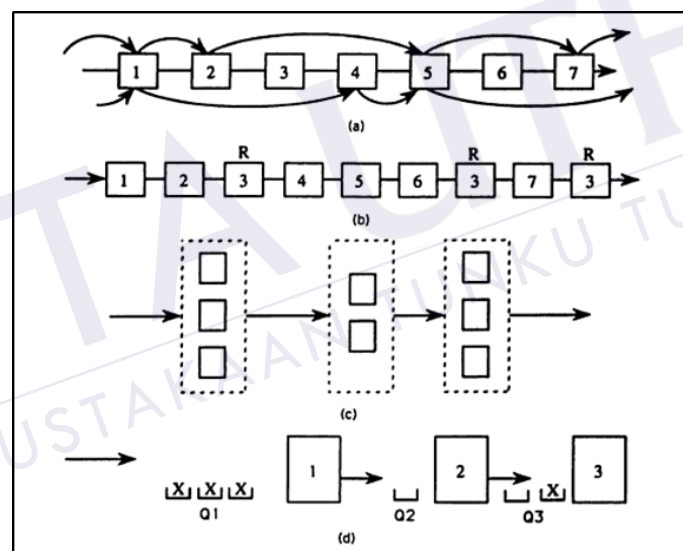


Figure 2.1: Flowshop scheduling illustrations (a) skip flowshop, (b) re-entrant flowshop, (c) compound flowshop, and (d) finite queue flowshop (Thomas and David, 1993)

2.2.2 Job shop scheduling

Job shop is the one that most commonly used in general production system. Job shop scheduling problems with setup times arise in many practical situations such as aerospace industries, fabrication industries, printing industries and semiconductor manufacturing industries (Sharma and Jain, 2015). There are several machines and jobs in the shop where some or all of machines were used in some specific sequence. Jobs are independent to each other. There is a restriction that a job cannot enter the machine more than once. Usually the main objective of job shop scheduling is to minimize the makespan or the tardiness penalty (Sule, 2008). Rui *et. al.*,(2014) used the efficiency of ant colony algorithm for solving the job shop scheduling problem.

A job shop is also known as a multi-stage production system where each job needs to undergo several operations to become a finished product. In a job shop, only a single machine is capable of processing each operation (Chiang and Lin, 2013). This caused blockage in production when any machine breaks down. According to Li *et. al* (2014), job shop scheduling problem can be generalized into the flexible job shop scheduling problem (FJSP) where two sub-problems are solved. The first one is called a routing sub-problem that assigns each operation to a machine selected from any of a set of suitable machines. The second one is called a scheduling sub-problem consisting of sequencing all the assigned operations on all machines in order to yield a feasible schedule to minimize a predefined performance criterion.

2.2.3 Open shop scheduling

For open shop scheduling, there is no operationally dependent sequence that a job must follow. A job may enter the machines in any sequence that the job needs (Sule, 2008). The term ‘open shop’ is often simply taken to mean a shop that rather than directly to customer order, it produces to final inventory. Just like the flowshop and job shop, the open shop scheduling problem consists of a set of n jobs to be processed on a finite set of m machines. In general, each job must be processed on every machine and consist of a series of m_i operations which have to be scheduled in

REFERENCES

- Abedinnia, H., Glock, C. H., and Brill, A (2016). New simple constructive heuristic algorithms for minimizing total flow-time in the permutation flowshop scheduling problem. *Computers & Operations Research*. 74: 165 – 174.
- Ahmad, S. S. S. (2009). *Bottleneck Adjacent Matching Heuristics for Scheduling a Re-Entrant Flow Shop with Dominant Machine Problem*. Universiti Tun Hussein Onn Malaysia: Ph.D. Thesis.
- Aldowaisan, T. and Allahverdi, A. (2003). New heuristics for no-wait flowshops to minimize makespan. *Computers & Operations Research*. 30: 1219 – 1231.
- Allahverdi, A. (2004). A new heuristic for m-machine flowshop scheduling problem with bicriteria of makespan and maximum tardiness. *Computers & Operations Research*. 31: 157 – 180.
- Allahverdi, A. and Al-Anzi, F.S. (2006). A branch-and-bound algorithm for three-machine flowshop scheduling problem to minimize total completion time with separate setup times. *European Journal of Operational Research*. 169: 767 – 780.
- Allahverdi, A. and Aldowaisan, T. (2002). New heuristics to minimize total completion time in m-machine flowshops. *International Journal Production Economics*. 77: 71 – 83.
- Bareduan, S. A. and Hasan, S. (2009). Bottleneck-based heuristic for re-entrant flow shop with two potential dominant machines. *Computers & Industrial Engineering*. 978: 4136 – 4244.
- Blum, C. and Andrea, R. (2003). Metaheuristics in combinatorial optimization: Overview and conceptual. *Journal ACM Computing Surveys*. 35(3): 268 – 308.

- Brah, S. A. and Loo, L. L. (1997). Heuristics for scheduling in a flow shop with multiple processors. *European Journal of Operational Research*. 113: 113 – 122.
- Braune, R and Zapfel, G. (2015). Shifting bottleneck scheduling for total weighted tardiness minimization. A computational evaluation of subproblem and re-optimization heuristics. *Computers & Operations Research*. 66: 130 – 140.
- Chakraborty, U. K. (2009). *Computational Intelligence in Flowshop & Jobshop Scheduling*. India: Springer Mathematics.
- Chakravarty, K. and Rajendran, C. (1999). A heuristic for scheduling in a flowshop with bicriteria of makespan and maximum tardiness minimization. *Production Planning and Control*. 10: 707 – 14.
- Chen, C. L. and Chen C. L. (2009). A bottleneck-based heuristic for minimizing makespan in a flexible flow line with unrelated parallel machines. *Computers & Operations Research*. 36: 3073 – 3081.
- Chiang, T. C. and Lin, H. J. (2013). A simple and effective evolutionary algorithm for multiobjective flexible job shop scheduling. *International Journal of Production Economics*. 141(1): 87 – 98.
- Dong, X., Huang, H., and Chen, P. (2008). An improved NEH-based heuristic for the permutation flowshop problem. *Computers & Operations Research*. 35: 3962 – 3968.
- Emmons, H. and Vairaktarakis, G. (2012). *Flowshop Scheduling: Theoretical Results, Algorithms, and Applications*. London: Springer Science and Business Media.
- Framinan, J. M. and Leisten, R (2003). An efficient constructive heuristic for flowtime minimisation in permutation flow shops. *Omega*. 31(4): 311 – 7.
- Framinan, J. M., Gupta, J. N. D., and Leisten, R (2004). A review and classification of heuristics for permutation flow-shop scheduling with makespan objective. *Journal of Operation Research Society*. 55(12): 1243 – 55.
- Framinan, J. M., Leisten, R. & Rajendran C. (2003). Different initial sequences for the heuristic of Nawaz, Ensore and Ham to minimize makespan, idle time or flowtime in the static permutation flowshop sequencing problem. *International Journal of Production Research*. 41(1): 121 – 128.

- Framinan, J. M., Leisten, R. & Rajendran C. (2006). A heuristic for scheduling a permutation flowshop with makespan objective subject to maximum tardiness. 99: 28 – 40.
- Gupta, J. N. D and Stanford, E. F. (2006). Flowshop scheduling research after five decades. *European Journal of Operation Research*. 169(3): 699 – 711.
- Ho, J. C and Chang, Y. L. (1995). Minimizing the number of tardy jobs for m parallel machines. *European Journal of Operation Research*. 84: 343 – 355.
- Isa, N. A. (2015). *Multiple Weightage Idle Time Heuristic for Flowshop Scheduling*. Universiti Tun Hussein Onn Malaysia: Bachelor's Degree Thesis.
- Johnson, S. (1954). Optimal two-and three stage production schedules with setup times included. *Naval Research Logistics Quarterly*. 1: 61 – 69.
- Kalczynski, P. J. and Kamburowski, J. (2005). A heuristic for minimizing the makespan in no-idle permutation flow shops. *Computers & Industrial Engineering*. 49: 146 – 154.
- Kalczynski, P. J. and Kamburowski, J. (2007). On the NEH heuristic for minimizing the makespan in permutation flow shops. *OMEGA, The International Journal of Management Science*. 35: 53 – 60.
- Kalczynski, P. J. and Kamburowski, J. (2008). An improve NEH heuristic to minimize makespan in permutation flow shops. *Computers & Operations Research*. 35: 3001 – 3008.
- Kalin, A. A. and Sarin, S. C. (2001). A near-optimal heuristic for the sequencing problem in multiple-batch flow-shops with small equal sublots. *International Journal of production Research*. 18(3): 345 – 357.
- Kenneth, R. B. and Dan, T. (2013). *Principles of Sequencing and Scheduling*. Canada: John Wiley & Sons.
- Koulamas, C. (1998). A new constructive heuristic for the permutation flow shop scheduling problem. *European Society*. 105: 66 – 71.
- Lee, L. (2000). *Zero Wait Flow Shop with Multiple Processors with Heuristics, Algorithm, and Mathematical Concepts*. University of Houston: Ph.D. Thesis.
- Li, J. Q., Pan, Q. K. and Tasgetiren, M. F. (2014). A discrete artificial bee colony algorithm for the multi-objectives flexible job shop scheduling problem with maintenance activities. *Applied Mathematical Modelling*. 38(3): 1111 – 1132.

- Marichelvam, M. K., Prabakaran, T. and Yang, X. S. (2014). Improved cuckoo search algorithm for hybrid flow shop scheduling problems to minimize makespan. *Applied Soft Computing*. 19: 93 – 101.
- Marti, R. and Reinelt, G. (2011). *The Linear Ordering Problem: Exact and Heuristic Methods in Combinatorial Optimization*. Springer Applied Mathematical Sciences.
- Martinez, K. Y. P. and Toso, E. A. V. (2015). Lot sizing and scheduling in the molded pulp packaging industry. *Gestao and Production*. 23(3): 104 – 112.
- Modrak V. and Pandian R. S. (2010). Flow shop scheduling algorithm to minimize completion time for n -jobs m -machine problem. *Technical Gazette*. 17(3): 273 – 278.
- Mukhopadhyay, S. K. (2015). *Production Planning and Control*. Delhi: PHI Learning Private Limited.
- Nagano, M. and Moccasin, J. J. (2002). A high quality solution constructive heuristic for flow shop sequencing. *Journal of the Operational Research Society*. 53: 1374 – 1379.
- Nawaz, M., Ensore, E. E. and Ham, I. (1983). A heuristic algorithm for the m -machine, n -job flow-shop sequencing problem. *OMEGA*. 11: 91 – 95.
- Osman, I. H. and Kelly, J. P. (1996). *Metaheuristics: Theory & Applications*. United State of America: Kluwer Academic Publishers Group.
- Pan, Q. and Ruiz, R. (2013b). A comprehensive review and evaluation of permutation flowshop heuristics to minimize flowtime. *Computer Operational Research*. 40: 117 – 128.
- Rahman, H. F., Sarker, R. and Essam, D. (2015). A genetic algorithm for permutation flow shop scheduling under make to stock production system. *Computers & Industrial Engineering*. 90: 12 – 24.
- Rajendran, C (1993). Heuristic algorithm for scheduling in a flowshop to minimize total flowtime. *International Journal Productivity Economy*. 29(1): 65 –73.
- Rajendran, C. (1995). Heuristics for scheduling in flowshop with multiple objectives. *European Journal of Operational Research*. 82: 540 – 555.
- Rajendran, C. and Ziegler, H (1997). A heuristic for scheduling to minimize the sum of weighted flowtime of jobs in a flowshop with sequence-dependent setup times of jobs. *Computers & Industrial Engineering*. 33(1-2): 281 – 284.

- Rajendran, C. and Ziegler, H. (1997). An efficient heuristic for scheduling in a flowshop to minimize total weighted flowtime of jobs. *European Journal of Operational Research*. 103: 129 – 138.
- Rui, Z., Shilong, W., Zheqi, Z. and Lili, Y. (2014). An ant colony algorithm for job shop scheduling problem with tool flow. *Journal of Engineering Manufacture*. 228(8): 959 – 968.
- Ruiz, R. and Maroto, C. (2005). A comprehensive review and evaluation of permutation flowshop heuristics. *European Journal of Operational Research*. 165: 479 – 494.
- Ryan, B. F., Joiner, B. L., and Cryer, J. D. (2012). *Minitab Handbook Updated for Release 16; Sixth Edition*. United States of America: Brooks/ Cole.
- Saleh, N. W. (2014). *Modified NEH Heuristic Scheduling by using Weighted Idle Time*. Universiti Tun Hussein Onn Malaysia: Bachelor's Degree Thesis.
- Sharma, P. and Jain, A. (2015). A review on job shop scheduling with setup times. *Journal of Engineering Manufacture*. 230(3): 517 – 533.
- Sule, D. R. (2008). *Production Planning and Industrial Scheduling; Examples, Case Studies and Applications; Second Edition*. United States of America: CRC Press, Taylor and Francis Group.
- Taillard. E. (1990). Some efficient heuristic methods for the flow shop sequencing problem. *Europe Journal Operation Research*. 47(1): 65 – 74.
- Tardos. E. (1986). A strongly polynomial algorithm to solve combinatorial linear programs. *Operations Research*. 34 (2), 250 – 256.
- Thomas, E. M. & David, W. P (1993). *Heuristic Scheduling Systems*. Canada: Wiley-Inter science.
- Valente, J. M. S. (2006). Local and global dominance conditions for the weighted earliness scheduling problem with no idle time. *Computers & Industrial Engineering*. 51: 765 – 780.
- Valente, J. M. S. and Alves, R. A. F. S. (2005). Improved heuristic for the early/tardy scheduling problem with no idle time. *Computers & Operations Research*. 32: 557 – 569.
- Viagas, V. F. and Framinan, J. M. (2015a). Efficient non-population-based algorithms for the permutation flowshop scheduling problem with makespan minimisation subject to a maximum tardiness. *Computers & Operations Research*. 64: 86 – 96.

- Viagas, V. F. and Framinan, J. M. (2015b). NEH-based heuristic for the permutation flowshop scheduling problem to minimise total tardiness. *Computers & Operations Research*. 60: 27 – 36.
- Viagas, V. F. and Framinan, J. M. (2015c). A new set of high-performing heuristics to minimize flowtime in permutation flowshops. *Computers & Operations Research*. 53: 68 – 80.
- Wegener, I. (2005). *Complexity Theory; Exploring the Limits of Efficient Algorithms*. Springer-Verlag Berlin Heidelberg.
- Woo, H. S. and Yim, D. S. (1998). A heuristic algorithm for mean flowtime objective in flowshop scheduling. *Computers & Operations Research*. 25(3): 175 – 182.
- Khafa, F. and Abraham, A. (2008). *Metaheuristics for Scheduling in Industrial and Manufacturing Applications*. Germany: Springer Science & Business Media.
- Yang, D. L. and Chern, M. S. (2000). Two-machine flowshop group scheduling problem. *Computers & Operations Research*. 27: 975 – 985.
- Zhang, R. and Wu, C. (2012). Bottleneck machine identification method based on constraint transformation for job shop scheduling with genetic algorithm. *Information Sciences*. 188: 236 – 252.
- Zainudin, A. M. (2017). *Dynamic Weighted Idle Time Heuristic for Flowshop Scheduling*. Universiti Tun Hussein Onn Malaysia: Master Degree Thesis.
- Zhenqiang, B., Weiye, W., Peng, W., and Pan, Q. (2012). Research on production scheduling system with bottleneck based on multi-agent. *Physics Procedia*. 24: 1903 – 1909.